

# New physics and signal-background interference in associated $pp \rightarrow HZ$ production

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**Abstract** – We re-investigate electroweak signal-background interference in associated Higgs production via gluon fusion in the presence of new physics in the top-Higgs sector. Considering the full final state  $pp \rightarrow b\bar{b}\ell^+\ell^-$  ( $\ell = e, \mu$ ), we discuss how new physics in the top-Higgs sector that enhances the  $ZZ$  component can leave footprints in the  $HZ$  limit setting. In passing we investigate the phenomenology of a class of new physics interactions that can be genuinely studied in this process.

**Introduction.** – After the Higgs discovery in 2012 and initial property measurements [1, 2] in the so-called  $\kappa$  framework, the phenomenology community has now moved towards understanding constraints in the dimension six effective field theory (EFT) extension of the Standard Model (SM), which provides a theoretically clean and well-defined approach to constrain the presence of new physics interactions with minimal assumptions [3–7].

The field of Standard Model EFT has seen a rapid development recently. Not only have the run I measurements by ATLAS and CMS been interpreted in terms of the dimension six EFT extension [8–26], but the EFT framework has also been extended to next-to-leading order [27–35]. Measurement strategies that take into account these corrections via renormalization group improved calculations have been presented in [36, 37].

Due to the large number of effective operators that are relevant to Higgs physics, it becomes essential to collect information from all possible processes related to the Higgs boson, especially at the LHC run II and the future high luminosity phase. Since a single effective operator can contribute to different processes, there are correlations among them that can be used to find bounds on the Wilson coefficients of different operators. Measurements of associated Higgs production [20, 36, 38], Higgs+jet production [39–45], top quark-associated and multi-Higgs [46–50] production and the recently developed Higgs off-shell measurements in  $gg \rightarrow ZZ$  [51–53] will be pivotal to obtain a

fine-grained picture of potential compatibility of the Higgs discovery with the SM expectation. In particular, the latter production mechanism has been motivated as an excellent candidate to constrain new physics effects by exploiting large momentum transfers to break degeneracies of new physics interactions in the on-shell Higgs phenomenology [54–57].

Similarly, high momentum transfers in associated Higgs production  $pp \rightarrow HZ$  are sensitive probes of new interactions [20, 58–60]. The reason is the existence of a destructive interference between the triangle and box contributions in the SM that can be lifted by new or anomalous couplings. Furthermore, the high momentum transfer provides another avenue to discriminate the Higgs signal from the background relying on jet substructure methods [61–65].

While jet-substructure analyses provide an extremely versatile and adaptable tool in new physics and Higgs searches, the mass resolution of Higgs decays  $H \rightarrow b\bar{b}$  in such a search is a limiting factor. This becomes a challenge especially if cross sections or beyond the SM-induced deviations thereof become small for large backgrounds.

It is known that gluon fusion-induced associated Higgs production [66–68], while only contributing  $\sim 10\%$  of the inclusive  $HZ$  production cross section [69–81], becomes relevant at large momentum transfers due to the top quark threshold [58, 59]. A similar argument applies to the non-decoupling of  $gg \rightarrow H \rightarrow ZZ$  at high mo-

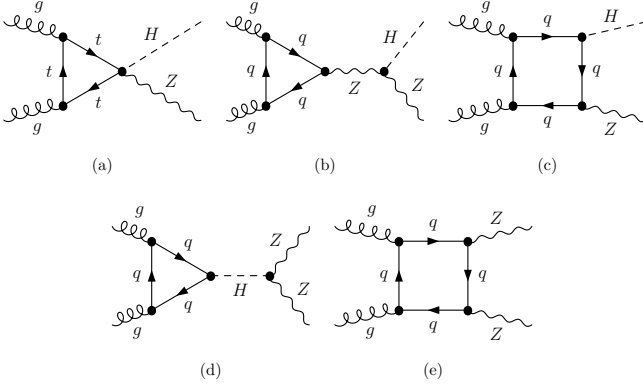


Fig. 1: Representative Feynman diagrams contributing to  $pp \rightarrow (H, Z)Z \rightarrow b\bar{b}\ell^+\ell^-$ ; we suppress the Higgs and  $Z$  boson decays.

momentum transfers [51, 52, 82]. Therefore the same type of physics can enhance both  $pp \rightarrow HZ$  and  $pp \rightarrow ZZ$ . We are therefore tempted to ask the following question: when studying the full final state  $pp \rightarrow b\bar{b}\ell^+\ell^-$  as signal for  $pp \rightarrow H(\rightarrow b\bar{b})Z(\rightarrow \ell^+\ell^-)$  \* for kinematics that allow the discovery of the Higgs boson in associated production, how important is the irreducible  $pp \rightarrow Z(\rightarrow b\bar{b})Z(\rightarrow \ell^+\ell^-)$  background keeping in mind an imperfect  $H \rightarrow b\bar{b}$  resolution?

To answer this question we organise this letter as follows. First we introduce a minimal set of operators which impact the two contributions  $pp \rightarrow HZ$  and  $pp \rightarrow ZZ$  in a different way, but necessarily related through gauge invariance. We then investigate the phenomenology of high  $p_T$  final states at the parton level. Subsequently, we show how our findings translate to the fully hadronized final state before we conclude.

**New physics effects in gluon initiated  $HZ$  production.** – Gluon-initiated associated production has been shown to contribute significantly to  $pp \rightarrow HZ$  in the boosted regime at the LHC and important consequences for new physics searches can be obtained by looking at this process [58, 59, 79]. New physics can potentially modify associated Higgs production both in the quark- and gluon-initiated channels. The quark-initiated channel may be altered at leading-order through modified Higgs couplings [37] or at next to leading-order through the influence of new particles or effective operators in loops [59, 83]. Similarly, the gluon-initiated channel may receive corrections through modified Higgs and top couplings to SM states.

In principle, all dimension six operators that are relevant for the Higgs sector should be considered since at the very least they can change the Higgs width, which affects the full partonic final state. However, several of these operators are already constrained from other observables, such as the  $Z$ -pole properties measured at LEP1. In order to keep our discussion transparent, we will focus on only

\*The Higgs decay to leptons, i.e.  $pp \rightarrow HH \rightarrow b\bar{b}\ell^+\ell^-$  is numerically negligible.

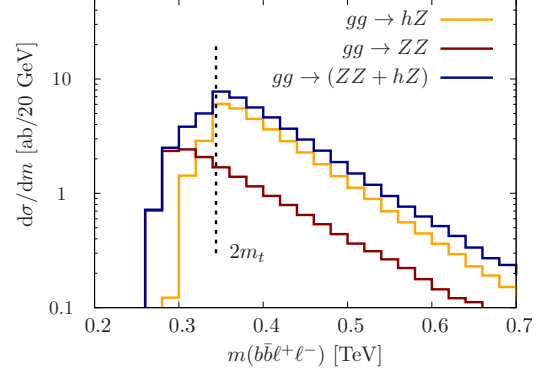


Fig. 2: Invariant mass distribution of the  $b\bar{b}\ell^+\ell^-$  (in this plot  $\ell = \mu$ ) system for the final state  $gg \rightarrow b\bar{b}\ell^+\ell^-$  in the SM and the phase space region  $p_T(\ell^+\ell^-) \gtrsim 100$  GeV relevant for a boosted  $H \rightarrow b\bar{b}$  analysis.

two operators that are weakly constrained and are relevant for Higgs production (we adopt the parameterisation of [7, 84, 85]):

$$\mathcal{O}_{Ht} = \frac{i\bar{c}_{Ht}}{v^2} (\bar{t}_R \gamma^\mu t_R) (\Phi^\dagger \overleftrightarrow{D}_\mu \Phi), \quad (1)$$

$$\mathcal{O}_t = -\frac{\bar{c}_t}{v^2} y_t \Phi^\dagger \Phi \Phi^\dagger \cdot \bar{Q}_L t_R + \text{h.c.} \quad (2)$$

with hermitian covariant derivative  $\Phi^\dagger \overleftrightarrow{D}_\mu \Phi = \Phi^\dagger (D_\mu \Phi) - (D_\mu \Phi)^\dagger \Phi$ , and  $\Phi$  being the weak doublet that contains the physical Higgs  $\Phi \supset H$ .

The operator in Eq. (1) modifies the coupling of the right-handed top quark to the  $Z$  boson  $\bar{t}_R t_R Z$  by a factor proportional to the  $\bar{c}_{Ht}$  coefficient

$$\frac{2}{3} g \frac{s_W^2}{c_W} \rightarrow \frac{2}{3} g \frac{s_W^2}{c_W} + g \frac{\bar{c}_{Ht}}{2c_W}. \quad (3)$$

It affects the  $Ztt$  coupling but not  $Htt$  and introduces a new  $ttHZ$  coupling. As required by gauge invariance, the derivative coupling of the top quark to the neutral Goldstone boson gets also shifted by the same quantity. Couplings to left-handed quark doublets are constrained by data on  $Z \rightarrow b\bar{b}$  and will not change the qualitative outcome of our discussion.<sup>†</sup> Operators of this form but involving light fermions are constrained by precision electroweak measurements  $|c_{Hu}| \lesssim 2\%$  and assuming a trivial flavor structure of the UV dynamics will directly constrain the interaction of Eq. (1), which is otherwise unconstrained at the tree level by electroweak precision data and has no impact on Higgs decays (see, e.g. [7] for a comprehensive discussion). Higher order corrections, however, re-induce a dependence, see [87]. We will ignore this potential constraint for the time being, but will come back to it later.

The operator in Eq. (2) modifies the top Yukawa coupling by a factor proportional to Wilson coefficient  $\bar{c}_t$ ,

<sup>†</sup>Interactions of this type can typically arise in composite Higgs scenarios [86], which will also leave footprints in  $q\bar{q} \rightarrow HZ$  as a function of the fine-tuning parameter  $v^2/f^2$ , where  $f$  is the pion decay constant analogue.

$y_t \rightarrow y_t(1 + \bar{c}_t)$ , while leaving the top mass as in the SM with a simple redefinition of the top quark field. The non-derivative couplings of the top quark to the neutral Goldstone boson are unchanged.

We show in Fig. 1 the relevant Feynman diagrams for  $pp \rightarrow HZ$  and  $pp \rightarrow ZZ$  ignoring the diagrams involving the unphysical Goldstone bosons. Note in particular the new effective vertex  $\bar{t}tHZ$  introduced by operator Eq. (1), not present in the SM, which gives rise to the Feynman diagram contribution to the gluon-initiated amplitude shown in Fig. 1 (a), and which may affect the cancellation between triangle and box diagrams for  $pp \rightarrow HZ$  in the SM, leading to an enhanced cross section. This cancellation is also impacted by the change in the top Yukawa coupling introduced by operator Eq. (2). In fact, the effect of a flipped top Yukawa coupling (i.e., with a coupling of opposite sign with respect to the SM, corresponding to  $\bar{c}_t = -2$ ) on  $pp \rightarrow HZ$  was studied in [60].

Together these operators provide a parameterisation that allow us to “template” the  $gg \rightarrow ZZ$  and  $gg \rightarrow HZ$  components of the full partonic final state  $pp \rightarrow b\bar{b}\ell^+\ell^-$  in a gauge invariant fashion, and therefore gives us a well-defined approach to study the signal-background interference in this final state. Note that since these operators only modify the  $t\bar{t}H$  and  $t\bar{t}Z$  couplings, they do not affect the tree-level  $q\bar{q} \rightarrow HZ$  process. Only the operator Eq. (2) changes the Higgs branching ratios (by a few percent in the relevant  $BR(H \rightarrow b\bar{b})$  in the cases explored here) and it has been taken into account.

The new interactions arising from Eq. (1) and Eq. (2) were implemented using FEYNRULES [88]. We calculate the one-loop gluon-initiated  $gg \rightarrow (HZ + ZZ) \rightarrow b\bar{b}\ell^+\ell^-$  production amplitudes using the FEYNARTS, FORMCALC and LOOPTOOLS [89, 90] framework which we interface with VBFNLO [91] to perform the phase space integration and generate events in the Les Houches standard and keep the full quark mass dependencies throughout. We pass these events to HERWIG++ [92] for showering and hadronization. The  $q\bar{q}$ -initiated process is simulated with MADGRAPH5 [93] using an identical input parameter setting and passed through HERWIG++ to obtain the full hadronic final state. The respective samples are normalised to the NLO QCD predictions of the SM [68, 69]. We use a  $K$ -factor of 1.2 and 1.8 for  $q\bar{q}$  and  $gg$ -initiated processes respectively. We focus on collisions at 13 TeV centre of mass energy.

*Parton level analysis.* Before we analyse the full hadron level, it is worthwhile to re-investigate the order of magnitude of expected interference effects between the  $gg \rightarrow HZ$  and  $gg \rightarrow ZZ$  parts in the full  $pp \rightarrow HZ + ZZ$  final state (see also [79] for an earlier discussion). To this end, we show in Fig. 2 the parton level comparison of the invariant mass distribution between  $HZ$  and  $ZZ$  production for gluon-initiated  $b\bar{b}\ell^+\ell^-$  (in this case  $\ell = \mu$ ) production. Note the rise of the cross section near the  $2m_t$  threshold. For these selection requirements we find a

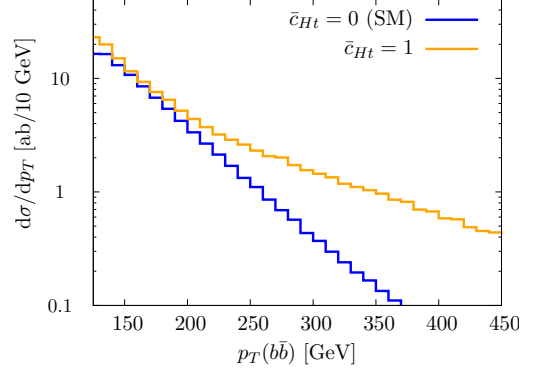


Fig. 3: Transverse Higgs  $p_T$  distribution and its sensitivity to the operator  $\bar{c}_{Ht}$ . It can be seen that the boosted regime  $p_T(\ell^+\ell^-) \simeq p_T(b\bar{b}) \gtrsim 150$  GeV is highly sensitive to the operator Eq. (1) which also modifies the continuum  $ZZ$  production.

SM cross section of 0.9 fb (including the flat  $K$ -factor). A choice of  $\bar{c}_{Ht} = 1, \bar{c}_t = 0$  increases this cross section by 70%. A quantitatively identical enhancement can be achieved for  $\bar{c}_{Ht} = 0, \bar{c}_t \simeq 0.33$ .

Signal-background interference between the two contributions is in general a small effect and the relative size of  $HZ$  dominates over  $ZZ$  as a consequence of the relative branching ratio suppression of  $H \rightarrow b\bar{b}$  (60%) and  $Z \rightarrow b\bar{b}$  (15%). This is left unchanged for changes in  $\bar{c}_t$  [79], however, there will be modifications from Eq. (2).

In order to obtain a first estimate of the sensitivity to the effective operators, we consider first the process  $pp \rightarrow (HZ + ZZ) \rightarrow b\bar{b}\ell^+\ell^-$  again at parton level. Based on the event simulation described above, we select events with

$$p_T(\ell^+\ell^-) > 150 \text{ GeV}, \quad 110 \text{ GeV} < m(b\bar{b}) < 140 \text{ GeV} \quad (4)$$

As an example, we show in Fig. 3 the effect of  $\bar{c}_{Ht} = 1$ . One can see that this operator can dramatically impact the boosted Higgs regime due to the lifting of the SM cancellation and also the derivative nature of the induced coupling [85].

In order to derive exclusion regions in the  $(\bar{c}_t, \bar{c}_{Ht})$  plane we perform a log-likelihood hypothesis test based on a shape comparison of the  $p_T(b\bar{b})$  distribution using the CL<sub>s</sub> method [94–96].

In Fig. 4 we show the expected exclusion for a luminosity of 100 fb<sup>-1</sup> based on our parton level results. While the resonant and continuum  $ZZ$  contributions are largely suppressed, the gauge-invariant extension of the top loop-induced  $gg \rightarrow ZZ$  diagram<sup>‡</sup> introduces the  $\bar{t}tHZ$  interaction. The result of Fig. 4 indicates that the modification according to operator Eq. (1), even for small choices in agreement with precision analyses [7] can in principle impact the limit setting procedure in associated Higgs production through sculpting the  $p_T(b\bar{b})$  distribution, especially when marginalising over Eq. (2) in a global fit where

<sup>‡</sup>One can understand the modification of the  $Zt\bar{t}$  interaction as replacing  $H \rightarrow \langle H \rangle$ .

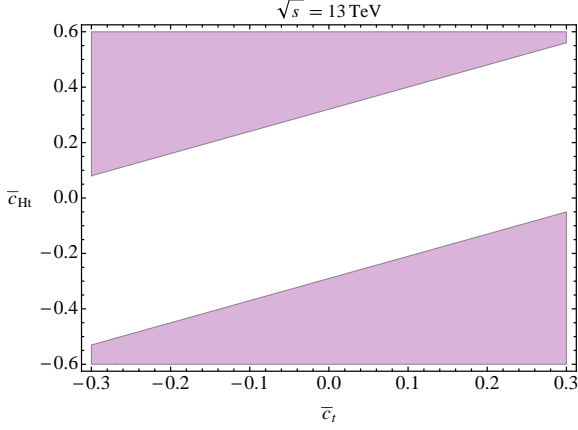


Fig. 4: Projected sensitivity of the boosted parton level analysis of  $pp \rightarrow b\bar{b}\ell^+\ell^-$  in the conventions of Eqs. (1) and (2), the shaded region is excluded at 95% confidence level for the ideal parton level setting described in the text, for  $\mathcal{L} = 100 \text{ fb}^{-1}$ .

degenerate operator directions will influence the expected exclusion.

One might worry about the validity of the Effective Field Theory in our analysis. This issue has been a subject of recent discussion, see e.g. [37, 97]. The coefficients of the dimension-6 operators can be related to the scale  $M$  where new physics appears by  $\bar{c} \approx g^2 v^2 / M^2$ , where  $g$  is a coupling constant of the heavy states with SM particles. Further suppression factors arise in the case in which an operator is generated at loop level. We can therefore put an upper bound in the new mass scale from requiring that the underlying theory is strongly coupled, i.e.,  $g = 4\pi$ :  $M < 4\pi v / \sqrt{\bar{c}} \approx 3 \text{ TeV}$  for  $c = \mathcal{O}(1)$ . Since our analysis relies on  $p_T < 1 \text{ TeV}$  we do not violate this upper bound.

*Showering and hadronization.* The results of the parton analysis detailed in the previous section are known to change substantially when we turn to the full hadron level final state and perform a realistic reconstruction [58]. Based on the event generation strategy outlined above, we apply typical  $HZ$  final state selection cuts by

- (i) requiring exactly 2 oppositely charged same-flavor leptons satisfying  $|\eta_\ell| < 2.5$ ,  $p_T(\ell) > 30 \text{ GeV}$ ,
- (ii) require that these leptons are compatible with the  $Z$  boson mass:  $80 \text{ GeV} < m(\ell^+\ell^-) < 100 \text{ GeV}$ ,
- (iii) and require boosted topologies  $p_T(\ell^+\ell^-) > 200 \text{ GeV}$ .
- (iv) We then perform a typical BDRS analysis [61]: All remaining hadronic activity is clustered using FAST-JET [98] into a Cambridge-Aachen fat jet with  $R = 1.2$ . The boosted Higgs candidate jet has to satisfy  $p_{T,j} > 200 \text{ GeV}$  and at least one such object is required in  $|\eta| < 2.5$ . The fat jet is filtered, mass-dropped and double b-tagged with a b-tag efficiency of 60% (2% fake rate), yielding a total efficiency of 36%.

- (v) Higgs candidates are required to be compatible with  $110 \text{ GeV} < m(b\bar{b}) < 140 \text{ GeV}$  evaluated on the b-tagged subjets.

While the high- $p_T$  selection is enough to remove the biggest background  $t\bar{t}$  almost entirely, jet-substructure approaches remove the QCD-induced  $b\bar{b}$  production modes from the selection to a large extent, leaving  $Z$ +jet production as a dominant background (or calibration tool). The Higgs mass resolution quoted in (v) is a key factor in the boosted analysis to allow signal vs. background extraction in the first place (and veto SM  $q\bar{q}$ -induced  $ZZ$  production). However as mentioned before the gluon-induced  $ZZ$  contribution could in principle be enhanced through the operator discussed previously, thus adding more significantly to the region (v) than expected in the SM and at parton level due to shower and hadronization effects.

After these analysis steps one typically obtains a cross section of  $\sim 0.2 \text{ fb}$  for the SM which includes both  $q\bar{q}$  and  $gg$ -initiated processes. And again we find the impact of  $HZ$  far more dominant than  $ZZ$ . As expected, the lowered statistical yield when taking into account the full reconstruction efficiencies requires a larger luminosity to set limits. Setting limits, we obtain a result comparable to the parton analysis of the previous section for  $3 \text{ ab}^{-1}$ , see Fig. 5. This means that when including the constraints from complementary Higgs measurements at this luminosity, which are expected to limit  $|\bar{c}_t| \lesssim 10^{-2}$  [26], the presence of  $\bar{c}_{Ht}$  for trivial flavor structures, i.e. at the level of  $\bar{c}_{Ht} = \bar{c}_{Hu}$  is difficult to constrain and can practically be neglected when working with this assumption. However, associated Higgs production provides test of non-trivial beyond the SM flavour structures, which can be combined with direct  $t\bar{t}Z$  searches (see e.g. [85, 87, 99–103]). Comparing to the projections of [99],  $-0.13 < \bar{c}_{Ht} < 0.64$ , we see that associated Higgs production can be expected to provide a additional discriminating power to comple-

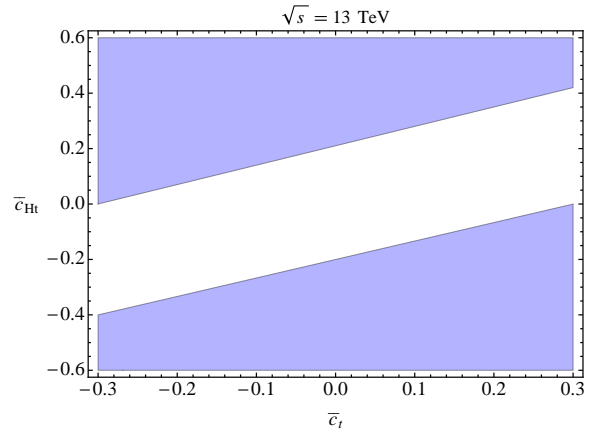


Fig. 5: Projected exclusion at 95% CL<sub>s</sub> (blue shaded region) of the boosted hadron level analysis of  $pp \rightarrow b\bar{b}\ell^+\ell^-$  at  $3 \text{ ab}^{-1}$  integrated luminosity.

mentary  $t\bar{t}Z$  searches. It should be noted that our results do not reflect systematic uncertainties from both theoretical and experimental sources and are therefore very likely to worsen, in particular in a global fit when more operators are included. In particular, the theoretical uncertainties due to missing higher orders in  $gg \rightarrow HZ$  are currently large for boosted kinematics  $\sim \mathcal{O}(30\%)$  [68]. Potential improvements in particular related to experimental systematics are hard to foresee at this stage in the LHC programme, but our results suggest that boosted Higgs analysis should continue to receive attention.

**Summary and Conclusions.** – In this letter we have re-investigated electroweak signal-background interference in gluon-initiated associate Higgs production in light of expected efficiencies and selection requirements of the fully hadronized final state. While  $HZ + ZZ$  signal-background interference is suppressed, new physics effects that impact  $pp \rightarrow ZZ$  can also leave footprints in boosted analyses  $pp \rightarrow HZ$  through new interactions related by gauge invariance. However, a robust limit setting in this channel will require a large luminosity. Even at these large luminosities the constraints on  $\bar{c}_{Ht}$  will not be competitive with electroweak precision constraints under the assumption of a trivial flavor structure (as commonly done in Higgs fits at this stage in the LHC phenomenology programme). Relaxing this assumption, associated Higgs production via gluon fusion can act as a test of this hypothesis, especially when other measurements point towards the SM.

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